

PROBLEM 1 *Symbolizing*

For each of the following, convert from text to symbolic logic. Some are known, named truths (we included the name for fun); others are false. The first one is done for you.

Celarent No G are F. All H are G. So: No H are F

$$\begin{aligned} \bar{\exists}x . G(x) \wedge F(x) & \qquad \text{or } \forall x . G(x) \rightarrow \neg F(x), \text{ or } \forall x . \neg(G(x) \wedge F(x)), \text{ or equivalent} \\ \forall x . H(x) \rightarrow G(x) & \qquad \qquad \qquad \text{or equivalent} \\ \therefore \bar{\exists}x . H(x) \wedge F(x) & \qquad \qquad \qquad \text{or equivalent} \end{aligned}$$

Barbara All G are F. All H are G. So: All H are F

$$\begin{aligned} \forall x . G(x) \rightarrow F(x) \\ \forall x . H(x) \rightarrow G(x) \\ \therefore \forall x . H(x) \rightarrow F(x) \end{aligned}$$

Ferio No G are F. Some H is G. So: Some H is not F

$$\begin{aligned} \bar{\exists}x . G(x) \wedge F(x) \\ \exists x . H(x) \wedge G(x) \\ \therefore \exists x . H(x) \wedge \neg F(x) \end{aligned}$$

(false) All G are F. No H is not G. So: Some H is not F

$$\begin{aligned} \forall x . G(x) \rightarrow F(x) \\ \bar{\exists}x . H(x) \wedge \neg G(x) \\ \therefore \exists x . H(x) \wedge \neg F(x) \end{aligned}$$

- No G are F. All H are G. So: No H are F

$$\begin{aligned} \bar{\exists}x . G(x) \wedge F(x) \\ \forall x . H(x) \rightarrow G(x) \\ \therefore \bar{\exists}x . H(x) \wedge F(x) \end{aligned}$$

- No G are F. Everything is F. So: Nothing is G

$$\nexists x . G(x) \wedge F(x) \quad \text{or} \quad \forall x . G(x) \rightarrow \neg F(x) \quad \text{or} \quad \forall x . \neg(G(x) \wedge F(x))$$

$$\forall x . F(x) \quad \text{or} \quad \nexists x . \neg F(x)$$

$$\therefore \nexists x . G(x) \quad \text{or} \quad \forall x . \neg G(x)$$

- All G are F. Something is G. So: Some G is F

$$\forall x . G(x) \rightarrow F(x) \quad \text{or} \quad \nexists x . G(x) \wedge \neg F(x) \quad \text{or} \quad \forall x . \neg G(x) \vee F(x)$$

$$\exists x . G(x)$$

$$\therefore \exists x . G(x) \wedge F(x)$$

Want more practice? Try Practice exercises $\forall x$ 22.A (pages 187–188)

PROBLEM 2 *Symbolizing with a Key*

Using this symbolization key:

domain: all animals

$A(x)$: ---_x is an alligator

$M(x)$: ---_x is a monkey

$Z(x)$: ---_x lives at the zoo

$L(x, y)$: ---_x loves ---_y

f : Fluffy

s : Slick

h : Howler

Symbolize each of the following sentences; the first one is done for you.

If both Slick and Howler are alligators, then Fluffy loves them both.

$$(A(s) \wedge A(h)) \rightarrow (L(f, s) \wedge L(f, h))$$

Any animal that lives at the zoo is either a monkey or an alligator.

$$\forall x . Z(x) \rightarrow (M(x) \vee A(x))$$

Howler loves a monkey.

$$\exists x . M(x) \wedge L(h, x)$$

All the monkeys that Fluffy loves love Fluffy.

$$\forall x . (L(f, x) \wedge M(x)) \rightarrow L(x, f)$$

Everyone Slick loves loves some animal other than Slick.

$$\forall x . L(s, x) \rightarrow (\exists y . (y \neq s) \wedge L(x, y))$$

Every animal in the zoo's love is outside the zoo, and vice versa.

$$\forall x, y . L(x, y) \rightarrow (Z(x) \oplus Z(y))$$

If both Slick and Howler are alligators, then Fluffy loves them both.

$$(A(s) \wedge A(h)) \rightarrow (L(f, s) \wedge L(f, h))$$

There are no monkeys at the zoo.

$$\begin{aligned} \forall x . Z(x) \rightarrow \neg M(x) \\ \text{— or —} \\ \nexists x . Z(x) \wedge M(x) \end{aligned}$$

Slick loves every animal that loves Slick.

$$\forall x . L(x, s) \rightarrow L(s, x)$$

Fluffy and Howler don't love any of the same animals.

$$\begin{aligned} \forall x . \neg L(f, x) \vee \neg L(h, x) \\ \text{— or —} \\ \forall x . L(f, x) \rightarrow \neg L(h, x) \\ \text{— or —} \\ \nexists x . L(f, x) \wedge L(h, x) \end{aligned}$$

Slick loves exactly one animal.

$$\exists x . \forall y . x \neq y \rightarrow L(s, x) \wedge \neg L(s, y)$$

Want more practice? Try Practice exercises $\forall x$ 22.B (page 188) and $\forall x$ 23.A–F (pages 199–203).