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CS 2102 - DMT1 - SPRING 2020 — LUTHER TYCHONIEVICH
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QUIZ 07

PROBLEM 1 *Convert to prose*

S : the set of all snakes

R : the set of all rabbits

$E(x, y)$: x eats y

$Y(x)$: x is yellow

Convert the following to simple, readable English:

1. $\exists r \in R . \forall s \in S . (E(s, r) \rightarrow \neg Y(s))$

There is a rabbit that no yellow snake eats.

PROBLEM 2 *Primes and factors*

2. $2 \cdot 3^2$ _____ is the prime factorization of 18

3. 3^4 _____ is the prime factorization of 81

4. $2^{20} \cdot 3^{40}$ _____ is the prime factorization of $9^{10} \cdot 6^{20}$

5. $\{1, 3, 7, 9\}$ _____ is the set positive 1-digit numbers relatively prime with 10

PROBLEM 3 *Proof by contradiction*

Prove the following using proof-by-contradiction. You may use prose or symbols or any readable mix of the two.

6. $\frac{7}{3} \notin \mathbb{Z}$

Proof.

We proceed by contradiction.

Assume $\frac{7}{3} \in \mathbb{Z}$; let $x \in \mathbb{Z}$ be the element of \mathbb{Z} that equals $\frac{7}{3}$. Thus, $\frac{7}{3} = x$, which can be re-written as $7 = 3x$. By the fundamental theorem of arithmetic, both must have the same prime factors, but 3 is a factor of x and is not a factor of 7, a contradiction.

Because assuming $\frac{7}{3} \in \mathbb{Z}$ led to a contradiction, it must be the case that $\frac{7}{3} \notin \mathbb{Z}$. \square